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## Motivation

- Autonomous multi-agent operations
- High-level task description → Automatic controller synthesis
- Reactive execution
- Fault accommodation

## Main Contributions

- System modeling using nondeterministic finite automata with  $\epsilon$ -transitions expressing the system's behavior and combining the agent's capabilities and constraints at the individual and group level, including failure modes.
- Determination of optimal task plans that satisfy any possible task specification from any initial condition, without the need to repeat the pre-processing cycle.
- Determination of reduced complexity sub-optimal solutions to the task planning problem.
- Incorporation of failure modes on-the-fly, after building the global system model (i.e. without the need to repeat the costly pre-processing step).

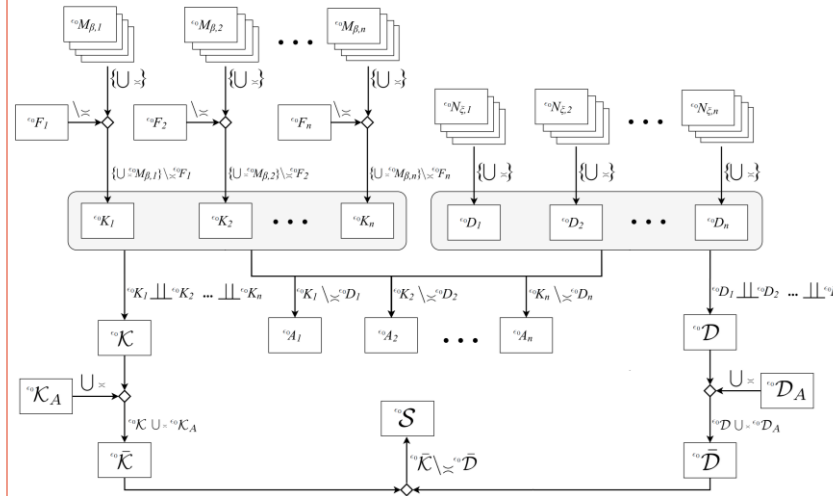
## Problem Statement

"Given a set of individual and inter-agents capabilities and constraints including their failure modes, the initial state of the system and a task specification, determine a string that provides an optimal execution (in terms of total transition cost) that brings the system from any initial state to any state satisfying the task specification."

## Some Important Definitions

- Definition 1:  $\epsilon_0$ -NFAs
- Definition 5: Compatible  $\epsilon_0$ -NFAs
- Definition 6: Union of Compatible Automata  $\cup_{\leq}$
- Definition 7: Subtraction of Compatible Automata  $\setminus_{\leq}$
- Definition 8: Concatenation of Compatible Automata  $\amalg_{\leq}$

## Agents' & Environment Models



## Problem Formulation

The **Task Specification** is a projection operation of the state space to the subspace of interest

With the **Environment Model** and the **Task Specification** we cast the problem as an instance of the Module Composition Problem

The solution to the Module Composition Problem enables us to seamlessly use the generated Module Chain as a modeled system for building Supervisory Controllers

## Completeness results

**Proposition 1**  
 With the proposed construction, the resulting environment model is complete

## Optimality results

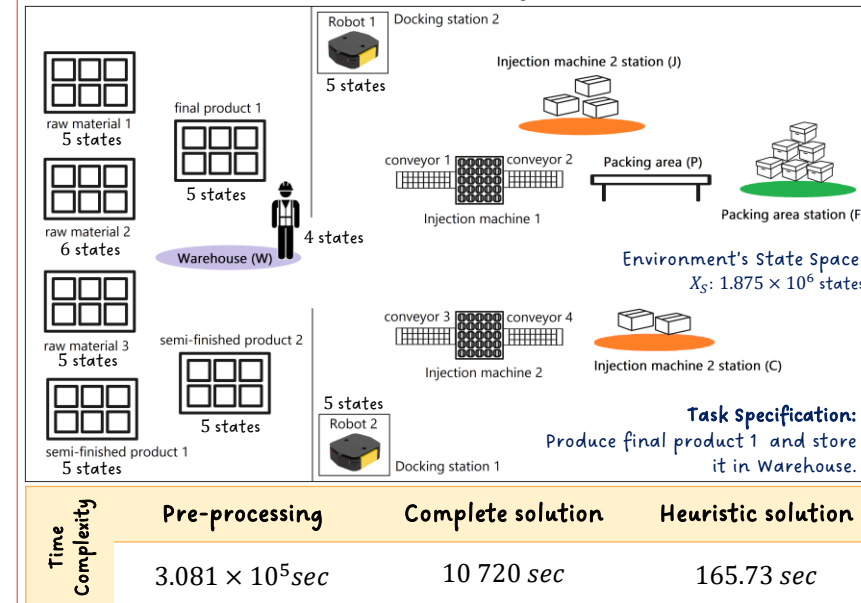
### Proposition 2

With the proposed construction, and assuming that only one agent is allowed to operate at any time instant, the solution produces the optimal sequence of actions to achieve the task specification.

## Analysis

- Time complexity to construct agents' models:  $O(|X_{A_i}|^2)$
- Time complexity to construct environment model:  $O(|X_S|^3)$
- On-the-fly incorporation of new failure modes (worst case time complexity):  $\prod_{i=1}^{n-1} |X_{A_i}|$
- Time complexity of complete algorithm:  $\frac{\prod_{i=1}^n |X_{A_i}|}{|X_{A_\sigma}|} \times O((V_S + E_S) \log V_S)$
- Time complexity of heuristic algorithm:  $O(E_S \log V_S)$

## Case Study



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